HYBRI D ROCKET COMBUSTI ON STUDY

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Abstract

1 he objectives of this study of "pure" or "classic" hybrids are to (1) extend our understanding of the boundary layer combustion process and the critical engineering parameters that define this process, (?) develop an up-to-date hybrid fuel combustion model, and (3) apply the model to correlate the regression rate and scaling properties of potential fuel candidates. I ests were carried out with a hybrid slab window motor, using several diagnostic techniques, over a range of motor pressure and oxidizer mass flux conditions. The results basically confirmed turbulent boundary layer heat and mass transfer as the rate limiting process for hybrid fuel decomposition and combustion, The measured fuel regression rates showed good agreement with the analytical model predictions, 1 he results of model scaling calculations to Shuttle SRM size conditions are presented.

Nomenclature

Arrhenius prefactor for fuel binder decomposition

 $\mathbf{a}_{\mathfrak{g}}$ constant in expression for gas emissivity

a_p - constant in expression for particle cloud emissivity

B - Spalding number

$$B = \frac{-}{C_{S}} (T_{S} - \frac{R_{g}^{\prime}}{T_{0}}) + \frac{R_{g}^{\prime}}{R_{g}} + \frac{R_{g}^{\prime\prime}}{R_{M}}$$
(1)

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b	•
Cs	specific heat of solid fuel
f',	activation energy for fuel binder decomposition
G	mass flux (total) through fuel port
G _{OX}	oxidizer mass flux at head-end of fuel port
K	convective heating constant
1	radiation path length
$N_{\rm p}$	particle number density
o/F	ratio of oxidizer/fuel mass flow rates
P	pressure
Pr	Prandtl number
OF	heat of decomposition of fuel binder
O_{m}	heat of fusion of aluminum
R	universal gas constant
r	fuel regression rate
r _{moan}	time and spatially averaged fuel regression rate
$T_{\mathfrak{g}}$	gas temperature
1 ₀	initial fuel bulk temperature
1 _P	radiating particle temperature

specific heat of combustion gases

 $\mathbf{c}^{\mathbf{b}}$

 $T_s \qquad \qquad \text{fuel surface temperature} \\ x \qquad \qquad \text{distance from head-end of fuel grain} \\ & & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & &$

 μ - gas viscosity

 ho_{i} density of fuel binder

 $ho_{
m s}$ density of solid fuel

o - Stefan-Boltzmann constant

Introduction

Hybrid rocket propulsion is of interest for advanced launch vehicle applications. It offers advantages of safety, lower cost, more benign combustion products, attractive performance, and mission flexibility relative to current rocket boosters.¹

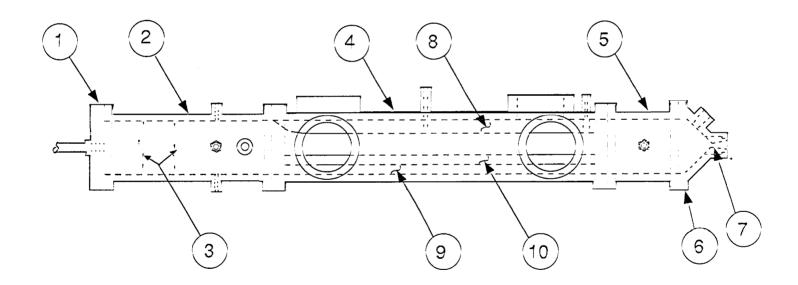
For the classical hybrid cycle (oxidizer injection into the forward end of an inert fuel grain) the combustion process occurs in a turbulent boundary layer diffusion flame. Extensive research in the 1960s²⁻⁵ demonstrated that for nonmetal containing fuels operating at normal pressures, > 1.75 MPa (250 psia), and oxidizer flow rates, the mixing anti reaction of the vaporizing fuel grain with the oxidizer flowing over the grain and transfer of heat back to the fuel surface is the overall rate-limiting process. In other words, the fuel regression rate is controlled by the fluid dynamics of the turbulent boundary layer established on the solid fuel surface. Classical hybrid regression rates tend, therefore, to be low, <0.25 cm/s (0.1 in./s), and dependent on the fuel' grain geometry. "This has an impact on the volumetric loading and utilization efficiencies of the solid fuel.

10 aid in the development of large-scale rocket motors, a study was initiated with the objectives of extending our understanding of the nature of the boundary layer combustion process (fuel decomposition, heat and mass transfer, and chemical reaction) and the critical engineering parameters that define this process and to develop an up-to-date hybrid fuel combustion model, based on models developed in the 1960s⁶, for guiding fuel developments, predicting regression rates in motors, and optimizing the design of hybrid rockets.

Test Program

1 he study is being carried out using a hybrid slab window motor system shown schematically in Figure 1. It consists of a (1) head-end closure, (2) flow straightener/igniter section with (3) flow straightening screens, (4) test





section with quartz viewing ports, (5) aft combustor section, (6) aft closure with (7) graphite nozzle, (8) internal spacer to control burner cross-sectional area, (9) fuel casting base plate, and (1 O) fuel slab. For a complete description of the system, the reader is referred to Ref. 7.

The fuel and oxidizer for this study are R-45M hydroxyl-terminated polybutadiene (H-I PB) and gaseous oxygen, respectively. 0.3% carbon is added to the HTPB to increase its radiation absorption coefficient. Tests were carried out over a pressure range of 1 to 2 MPa (140 - 280 psia) and head-end oxidizer mass flux (mass flow/port area) range of 0.7 to 7 gm/cm²-s (0.01 - 0.11bm/in²-s). Besides measurement of burner mean pressure and temperature lower limit (tungsten-rhenium thermocouple), combustion behavior diagnostics consist of motion picture and high speed digital video (4000 images/s) coverage through the forward and aft viewing ports. The time-averaged fuel regression rates were determined by both before and after measurement and weighing of the fuel slabs.

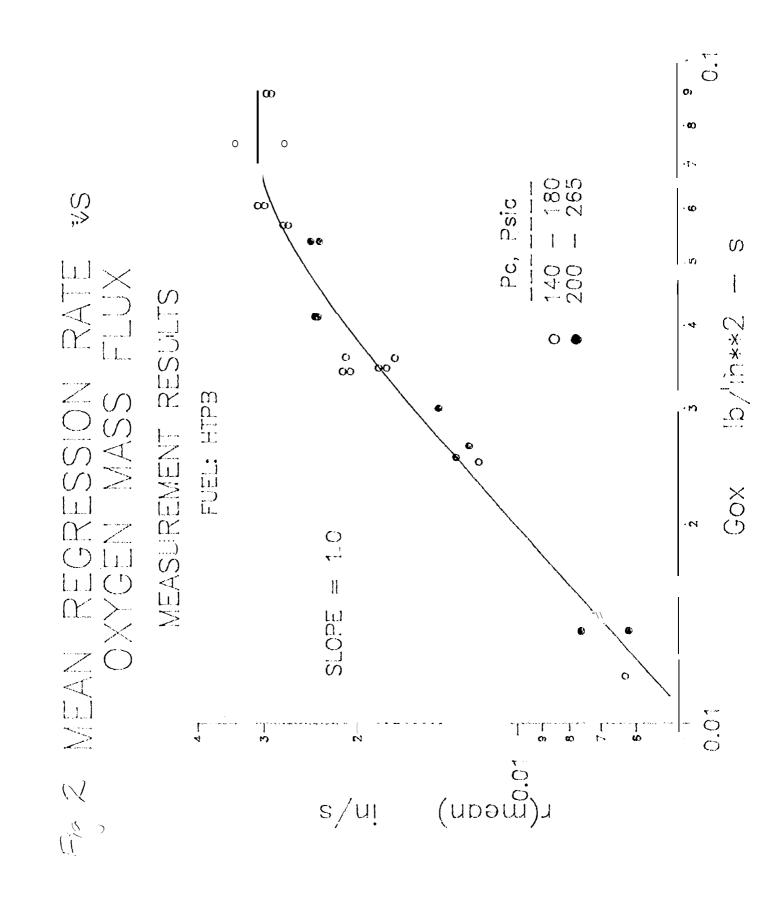
A hot wire anemometer was inserted in one of the spark plug igniter ports, and the turbulence level of the gaseous oxygen (GOX) core flow into the motor test section was measured under cold flow conditions duplicating the actual test oxygen mass flows and chamber pressures.

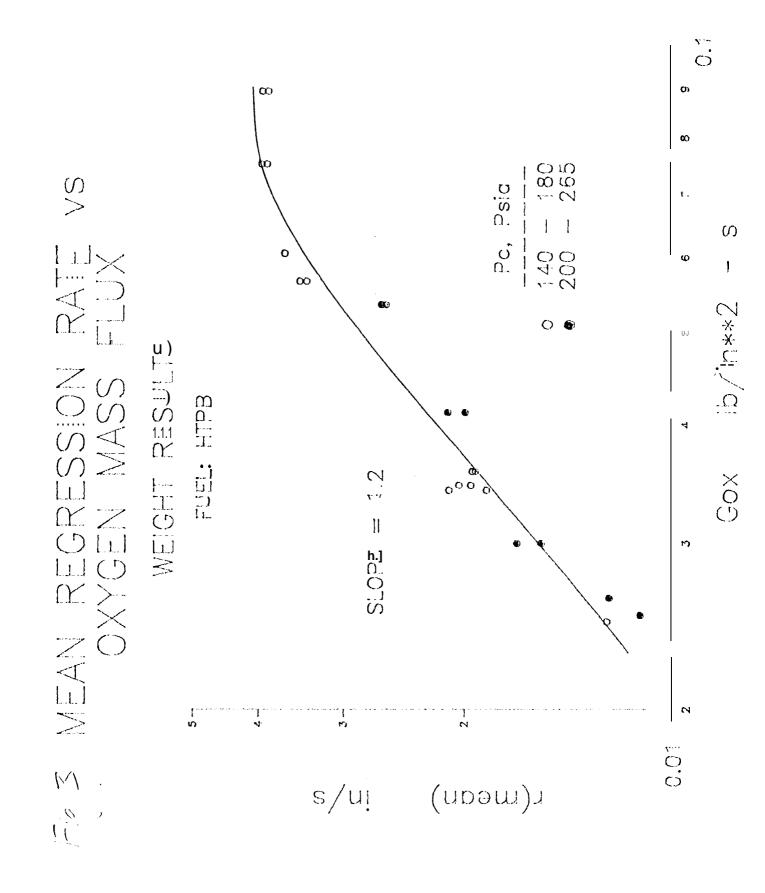
Test Results

Fuel Regression Rate

-Mean!-c-orrelat! On

Figure ? shows $r_{mean'}$ as calculated from before and after measurement of the fuel slabs, plotted versus time-averaged $G_{\rm OX}$. The data points are separated into the two indicated chamber pressure ranges. A power law curve fit yielded an exponent of unity. Plotted in this manner, the exponent is a function of the motor configuration, As will be shown later, plotting $r_{\rm mean}$ versus the total mass flux resulted in the near-0.8 power law dependence predicted by turbulent boundary layer diffusion flame theory. Figure 3 shows the results as calculated from before and after weighing of the fuel slabs, The regression rate was observed to be independent of pressure over the $G_{\rm OX}$ range tested. For the lower test-pressure range at least, the dependence on $G_{\rm OX}$ diminishes at the upper test values. 1 his indicates that





another process, probably the flame chemical kinetics, is becoming rate-limiting.⁸ This will be discussed further in the analytical model section,

Spatial Dependence

Figures 4 and 5 show the initial and post-test average thickness versus axial position profiles for two fuel slabs that were each used in five test firings, 1 he respective test mean $G_{\rm ox}$ values are indicated, At these $G_{\rm ox}$ levels the results show little variation in regression with axial position, except at the 1/4length position, From the high speed video results and the hollowed out, surface melt nature of the quenched surface, this augmented regression appears to be due to turbulent mixing enhancement resulting from vortices shed from the slab forward face.

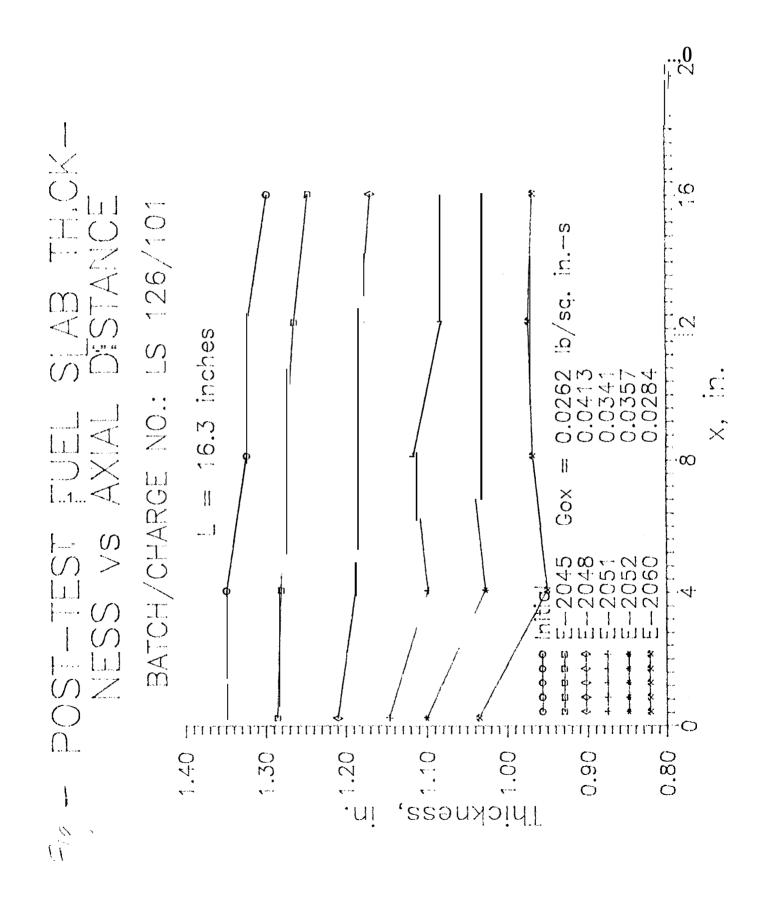
Turbulence Magnitude

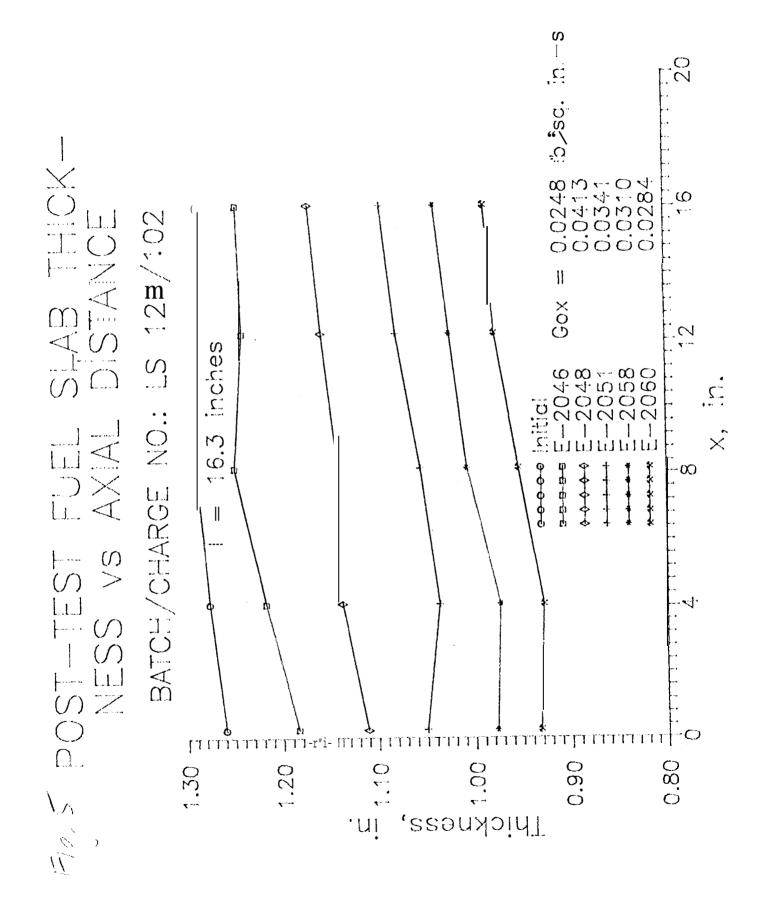
Figure 6, a portion of the achot wire anemometer trace for a cold flow test at a Gox of 6.4 gm/cm²-s (0.09 lb/in²-s) and motor chamber pressure of 1.9 Mf'a (275 psia), shows typical results. The amplitude of the oscillations is approximately 10% of the flow mean velocity. Analysis of the spectral density power showed broad-b and content decreasing logarithmically with frequency. 1 his broad-band content should also be characteristic of the corresponding hot-flow test condition.

Irregular Combustion

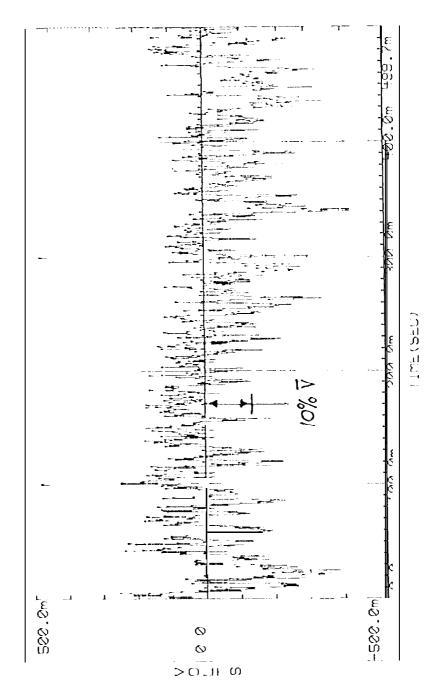
1 he pressure traces for most tests exhibited low-frequency, sub-acoustic pressure oscillations in varying degrees of strength. Figure 7 depicts the largest amplitudes observed to date. These bulk-mode oscillations are believed to be a motor chamber mass filling-venting phenomenon similar to solid rocket L*-instability. For the test conditions depicted in Figure 7, an approximate L*-instability calculation, adapting the theory of Beckstead and Price, predicted a pressure oscillation frequency of 3 to 4 Hz.

As to the source of this irregular combustion, tests reported elsewhere 10 indicate that it is not due to the oxygen feed, or turbulence induced by the step at the aft end of the slabs, or the combustion of the mixture in the aft-combustor volume. I-he remaining, actual driving mechanism is speculated to be some type of flow-combustion turbulence interaction along the surface of the fuel slab,

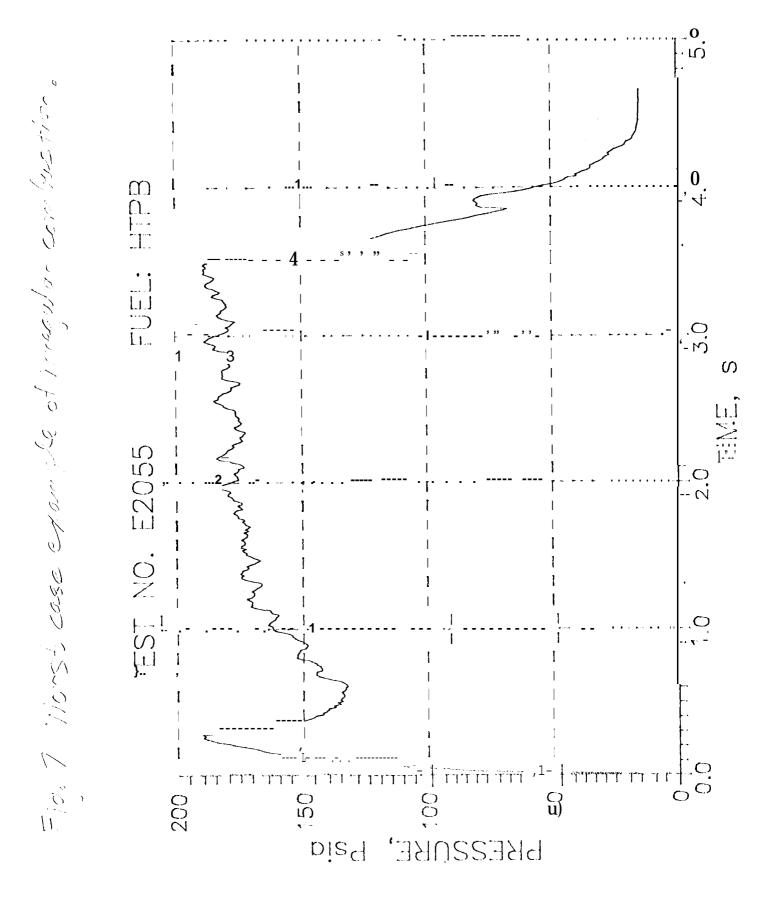




JET PROPULSION LABORATORY HYBRID COLD-FLOW TEST RUN E-2065 TURBULENCE MAGNITUDE



For Good flow were much of GOX had and will bere mark of take.



Analytical Combustion Model

Analysis of the Condensed Phase

The models of the 1960s⁶ lacked an adequate description of the condensed phase. The energy balance was lumped into an empirical parameter, the kinetics of fuel decomposition was not considered, and the surface temperature of the fuel was an assumed input quantity. Current knowledge enables these deficiencies to be remedied.

1 he energy balance at the fuel surface for a metal (Al) containing fuel can be written as:

$$\rho_s r [c_s (T_s - T_o) + \alpha_r Q_r + \alpha_{AL} Q_m] = \Phi_c + \Phi_R$$

(1)

The regression rate of the polymer is governed by Arrhenius kinetics:

$$\rho_F x = A_F \exp\left(-\frac{F_F}{RT_S}\right) \tag{2}$$

Kinetics constants, thermal properties, and heats of decomposition have been measured for a variety of polymers of interest.¹¹

Analysis of the Gas Phase

I he regression rate of the fuel is driven by heat transfer from the combustion zone in the gas phase. It is well-settled that there are two primary modes of heat transfer under the conditions of practical interest. First, convective transport from the turbulent boundary layer diffusion flame as modified by the surface transpiration (blowing) of the fuel binder, Second is radiation from the gases (and particulate clouds for metal containing fuels) that fill the fuel port cavities, It has been established that radiation is the primary mechanism for the pressure dependence of fuel regression rate under pressure conditions of practical interest. 6 Reaction kinetics do not contribute to a pressure dependence under these conditions because they are much faster than the ratelimiting diffusion process. Absent radiation, regression rates are dependent upon local mass flux and length position in accordance with turbulent convective transport theory.

1 he gas phase model of Smoot and Price³ was cast into the following expression to describe the convective heating component of the energy balance equation:

$$\phi_C = \{C_S (T_S - T_0) - \alpha_F Q_F + \alpha_{AL} Q_m\}$$

$${KG^{0.8} \left(\frac{\mu}{x} \right)^{0.2} \ln \left(\frac{\pi}{r^{2/3}} \right)}$$
 (3)

Radiation components are expressed as:

$$\Phi_{R,g} = \sigma T_g^A (1 - e^{-a_g P I}) \tag{4}$$

$$\Phi_{R,p} = \sigma T_p^A (1 - e^{-a_p N_p})$$
(5)

Radiation measurements for the combustion products of the test propellant systems are in preparation. In the absence of {measurements, the following assumptions were made to determine the emissivities. For the gases, data reported for a high energy non-aluminized solid propellant formulation were used to obtain values for $a_{\rm g}$. It turned out that radiation from the gases was negligible in the slab combustor tests, as confirmed by the absence of that type of pressure effect in Figures 2 and 3. For the aluminum particle cloud it was assumed that all the aluminum burned efficiently to fine aluminum oxide smoke, and data from solid propellant exhaust plumes 13 . 14 were used to quantify $a_{\rm p}$. Combining this with an expression for the number density of the oxide smoke particles, the result was:

$$a_p N_p = 0.00141 \xrightarrow{\sim_{AL} P} (6)$$

This radiation component was significant in previous slab motor tests carried out with a heavily aluminized (40% by weight) HTPB fuel, confirmed by the pressure dependence of the regression rates.⁷

Discussion

The foregoing equations can be combined to iterate for regression rate and surface temperature. They are of a form that has been used in the past to correlate and scale hybrid fuel regression rate data. They are also instructive. For example, regression rates can be increased by using a binder having a low heat of decomposition and by filling it with a significant fraction of particulate that would provide strong radiation components. Moreover, the greater the influence of the particulate, the less the regression rate will depend upon the local mass flux.

Model Calculations

HTPB Fuel

Figure 8 presents the fit to the HT PB fuel regression rate data, plotted here versus the time- arid spatially-averaged total mass flux, together with results of model calculations. To give this work some perspective, past data for other fuels are included.

The data show the classical near-0.8 power law dependence of fuel regression rate on mass flux. Data for conditions leading to a kinetics pressure dependence (high mass flux, low pressure) were omitted. The model is observed to be in very good agreement with the data for the HTPB binder fuel.

The effect of the fuel composition on regression rate is interesting. From plexiglass to HTPB there is a factor of 3 increase in regression rate. Understanding the reason for this difference could be useful to the development of improved fuels. Unfortunately, relevant data for plexiglass in the context of this model were not available. However, data for Butarez are available to help explain the lower regression of the butylrubber fuel compared to the HIPB of this work. Butarez has a higher specific heat, higher heat of decomposition, and slower decomposition kinetics than HTPB.7 hese tend to lower regression rate. Other factors may have been present, such as a lower flame temperature under the conditions of the butyl rubber tests. changes in binder properties were input into the model and the results are included in Figure 8. It is observed that the model can explain most, but not all, of the difference in the regression rate between butyl rubber and HTPB.

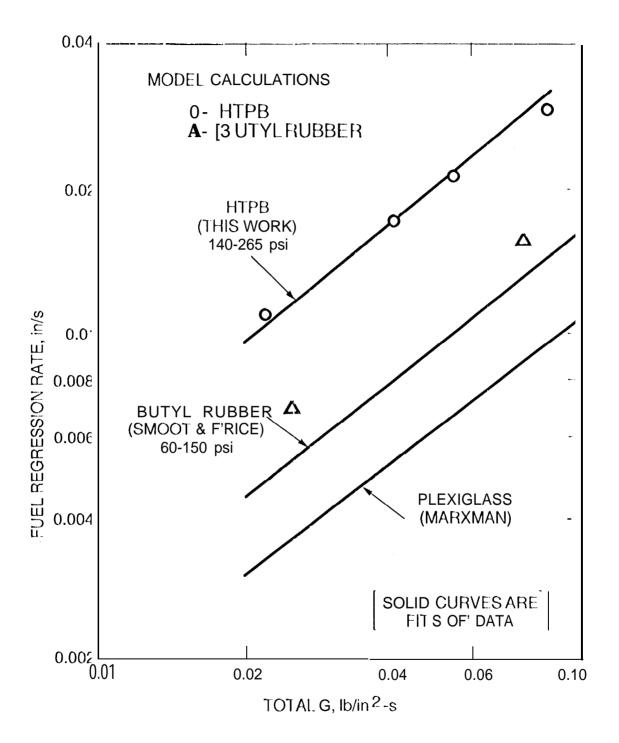


Fig. 8 Regression valor of vore mutalized lasts, and results of model calculation's (COX injection).

MetallizedHTPB Fuel

Figure 9 presents fits to the metallized (40% AI, 30% coal, 30% HTPB) hybrid fuel regression rate data' together with results of model calculations. These fillers increase the density of the fuel from 0.922 (HTPB alone) to 1,64 gm/cc, reduce the specific heat from 0.434 to 0.299 cal/gm-°K, and reduce the effective heat of decomposition of the fuel from 433 to 166 cal/gm. The dashed line extending the lower data curve is merely to illustrate the appearance of a classical 0.8 power law dependence, and is neither data nor a model result. Compared to the dashed line, the data fits and model results show a dependence that is less than 0.8. I-his is due to the effect of radiation, which becomes a stronger heat transfer contributor at lower values of G.

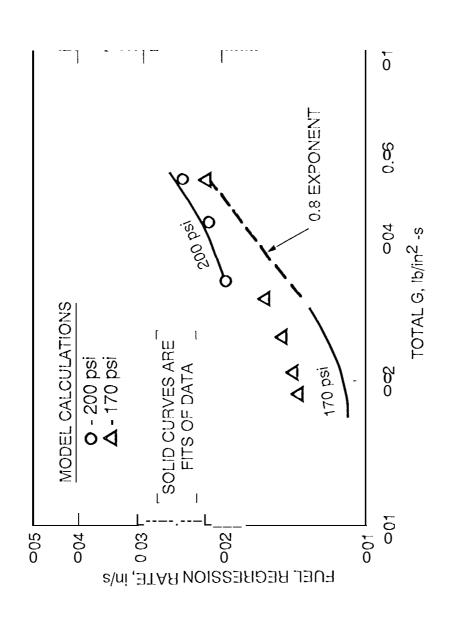
In modeling the coal filler it was assumed that the coal burned efficiently, such that it lost its particulate character and became part of the gas composition.

The model is observed to be in very good agreement with the higher pressure data, but overpredicts the regression rates at the lower pressure condition. 1 hus the pressure-sensitivity is greater in the data than predicted by the model. A possible explanation is an effect of pressure on aluminum combustion efficiency. At the lower pressure, a less efficient aluminum combustion would produce a lower number density of oxide smoke and therefore a reduced radiation component. At present, there is no basis for distinguishing larger unburned aluminum particles from the oxide smoke in the analysis.

The model predicts a reduced pressure sensitivity with increasing G, which is the expected result. This would also be shown by the data if the lower pressure data would more or less follow the dashed line extrapolation. However, it is possible that this higher exponent behavior would be followed because of improved aluminum combustion with increasing G, and not merely because of the growing dominance of convective heat transfer. Thus the model can be useful for data interpretation.

Scaling Calculations

Figure 10 represents the results of model calculations for the two fuels as scaled to Shuttle SRM booster conditions, together with the model results under the slab corn bustor conditions of lower pressure and lower G. The Shuttle SRM starts out at a pressure of 6.3 MPa (900 psi) at its initial web, and then provides a generally declining pressure with web burned to a final pressure of 2.8 MPa



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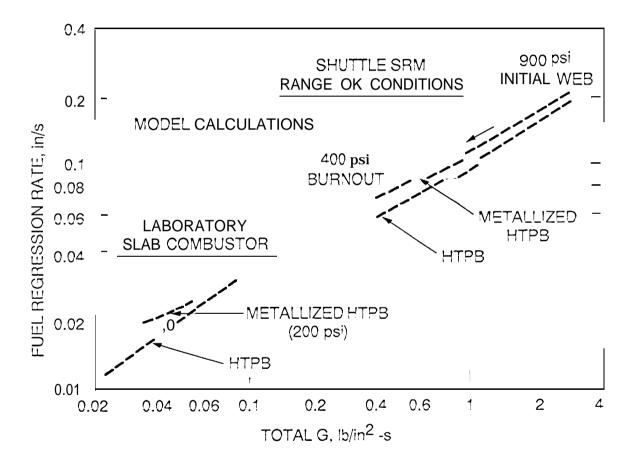


Fig. 10 Producted scaling of 1508 hole to 59th conditions,

(400 psi) near burn-out. The arrow on the figure denotes this path of operation. Note that the G range of operation is nearly two orders of magnitude greater, and that pressure is more than doubled, relative to the slab combustor. The scaled regression rates computed are values at the motor mid-length; this length scales to an amount comparable to the spatially averaged G.

It is predicted that radiation is significant in the SRM size, even for the unmetallized fuel, because of the greater path length as well as the higher pressures. 1 hus the G-dependence (slopes) of the two fuels are comparable in the SRM size, and are more like 0.6 than 0.8. This shows that radiation can still be effective at very high values of G if it is strong enough. The metallized fuel is predicted to burn faster because of its stronger radiation and lower enthalpy of decomposition.

Conclusions

1 he HTPB fuel results from this study (fuel regression rate dependence on G and non-dependence on P) confirm turbulent boundary layer heat and mass transfer as the rate limiting process for hybrid fuel decomposition and combustion under pressure conditions of practical interest. 1 he nature of the fuel surface decomposition is altered (from dry to a surface melt) and the rate of regression is enhanced by augmentation of the boundary layer turbulent mixing. I-he observed weak dependence of fuel rate of regression on motor axial position also supports classical theory.

As a boundary condition for future fluid dynamic analysis of the slab motor, the amplitude of the GOX inlet core-flow turbulence was approximately 10% of the mean velocity in cold-flow simulation tests.

The driving mechanisms for the bulk-mode pressure oscillations observed in these tests is speculated to be some type of flow-combustion turbulence interaction along the surface of the fuel slab,

An analytical model has been developed and applied to explain the regression rate behavior of non-metallized and metal lized HTPB fuels. Future slab combustor experiments will employ heat transfer sensors to sort out and correlate convective and radiative heating components for hybrid combustion products.

Model calculations with the test propellants were scaled to Shuttle SRM booster conditions. The scaled fuel regression rates are still lower than SRM solid propellant burn rates and too dependent on geometry. However, desired regression rate properties appear to be within reach, and continued fuel developments should enable more efficient motor designs to be achieved.

Acknowledgments

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